

## Exercise Set 9

**Exercise 9.1.** Consider an instance of the MULTISECTION PROBLEM with  $k$  regions and a feasible fractional assignment. Prove that there is an integral partition which violates capacity constraints by at most

$$\frac{k-1}{k} \max \{\text{size}(C) : C \in \mathcal{C}\}.$$

(5 points)

**Exercise 9.2.** Consider the fractional MULTISECTION PROBLEM with  $k = 2$  regions. Provide an alternative, simple (not using network flows)  $\mathcal{O}(n \log n)$  algorithm that computes an optimum fractional partition with the additional property that all but one circuit are assigned to only one region.

(5 points)

**Exercise 9.3.** Formulate the SIMPLE GLOBAL ROUTING PROBLEM as an integer linear program with a polynomial number of variables and constraints.

(5 points)

**Exercise 9.4.** Provide an instance of the SIMPLE GLOBAL ROUTING PROBLEM which admits a fractional solution, but no feasible integral solution. Your instance has to satisfy  $w(N, e) \leq u(e)$  for each net  $N$  and edge  $e$ .

(5 points)

**Deadline:** July 4<sup>th</sup>, before the lecture. The websites for lecture and exercises can be found at

<http://www.or.uni-bonn.de/lectures/ss17/chipss17.html>

In case of any questions feel free to contact me at [ochsendorf@or.uni-bonn.de](mailto:ochsendorf@or.uni-bonn.de).